Abstraction and Model Checking in the PEPA Plug-in for Eclipse

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Abstract—The stochastic process algebra PEPA is widely used for performance modelling, and a large part of its success is due to its rich tool support. As a compositional Markovian formalism, however, it suffers from the state space explosion problem, where even small models can lead to very large Markov chains. One way of analysing such models is to use abstraction — constructing a smaller model that bounds the properties of the original.

We present an extension to the PEPA plug-in for Eclipse that enables abstracting and model checking of PEPA models. This implements two new features. The abstraction view provides a graphical interface for labelling and aggregating states of individual PEPA components. The model checking view provides an interface for constructing CSL properties, which are then verified with respect to the specified abstraction. We have an internal CSL model checker for CTMDPs, so the tool can be used as a stand-alone.

I. INTRODUCTION

The Performance Evaluation Process Algebra (PEPA) [5] is a language for modelling systems in which a number of interacting components run in parallel, and whose behaviour is stochastic. The core semantics of PEPA is in terms of Continuous Time Markov Chains (CTMCs), and an alternative semantics in terms of Ordinary Differential Equations (ODEs) has also been developed. PEPA has been applied in practice to a wide variety of systems, and its success as a modelling language has been largely down to its extensive tool support. Most recently, the PEPA Plug-in Project [11] has integrated a range of analysis techniques — based on both numerical solution and simulation — into a single tool built on top of the Eclipse platform [1].

As with all compositional Markovian formalisms, however, PEPA suffers from the state space explosion problem. A model can have an underlying state space that is exponentially larger than its description, meaning that it can be infeasible to analyse. Fluid flow approximation using PEPA’s ODE semantics can solve this problem if we are only interested in the average behaviour of the system over time. However, if we want to reason over all possible behaviours of the model — for example, the probability that an error occurs within some time interval — then we must consider the CTMC semantics.

In this paper, we present a new extension to the PEPA plug-in, in which a model can be abstracted by combining, or aggregating, states. To safely over-approximate the behaviour of the original model (for any aggregation of its states), we use two abstraction techniques — abstract CTMCs [9] (a type of Markov decision process with infinite branching), and stochastic bounds [4]. We provide a model checker for the three-valued Continuous Stochastic Logic (CSL) [2], which computes from the abstraction a safe bound of the probability of a quantitative property holding in the original model — if the actual probability is $p$, then the model checker will return an interval $I = [p_1, p_2]$ such that $p \in I$.

The current version of the PEPA plug-in can be downloaded from http://www.dcs.ed.ac.uk/pepa/tools/plugin and provides two new views:

1) The Abstraction View is a graphical interface that shows the state space of each sequential component in a PEPA model. It provides a facility for labelling states (so that they can be referred to in CSL properties), and for specifying which states to aggregate.

2) The Model Checking View is an interface for constructing, editing, and model checking CSL properties. The property editor provides a simple way to construct CSL formulae, by referencing the labels given to states in the abstraction view. It ensures that only syntactically well-formed CSL formulae can be constructed.

Figure 1 shows a screenshot of the abstraction view in use.

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II. ABSTRACTION AND MODEL CHECKING OF PEPA

Our motivation behind the abstraction view is to allow the modeller to experiment with different aggregations of states in a fast and straightforward way. Since we support compositional abstractions, and the number of states in a single sequential PEPA component is usually small, it is possible to do so graphically. The user simply selects a number of states in a component, and clicks the “aggregate” button. The states can be separated again by clicking “disaggregate”. The same graphical interface is also used to compositionally label sets of states in the model.

Fig. 2. The CSL property editor

To construct CSL formulae, we provide an editor, which is illustrated in Figure 2. Labels from the abstraction view are made available as atomic properties, and we support both the path and steady state CSL operators. Once a property is specified, it can be verified in the model checking view, using the currently specified abstraction. If the result is not precise enough, a different abstraction can be constructed, and the property checked again. Importantly, the model checker always returns a safe probability interval in the case of quantitative properties, and a safe answer of ‘true’, ‘false’, or ‘maybe’ for Boolean properties, with respect to the original model.

Fig. 3. Architecture of the abstraction and model checking features

We have presented an extension to the PEPA plug-in for Eclipse, which allows compositional abstraction and CSL model checking of PEPA models. To put this in the context of other tools, PRISM [7] supports CSL model checking of (non-abstracted) PEPA models and MRMC [8] supports model checking of the CSL time-bounded until operator on CTMDPs, but not the abstraction of higher-level formalisms.

In the near future, we plan to extend our tool with support for the derived CSL operators (F, G, etc.) and the PEPA aggregate combinator, and to provide the ability to export to MRMC. The biggest limitation at present is that properties and abstractions cannot be saved and loaded alongside PEPA models, and we hope to implement this functionality soon.

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REFERENCES


1Note that we do not support the time-bounded next operator.

2PRISM does not support PEPA’s active-active synchronisation.